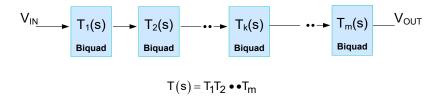
EE 508 Lecture 33

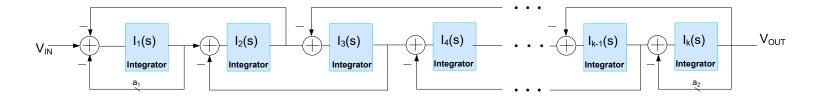
Leapfrog Networks

Filter Design/Synthesis Approaches

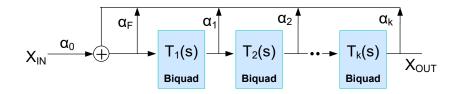
Cascaded Biquads



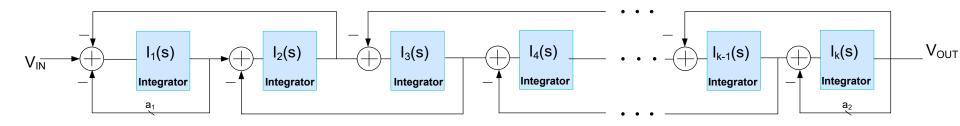
Leapfrog



Multiple-loop Feedback - One type shown



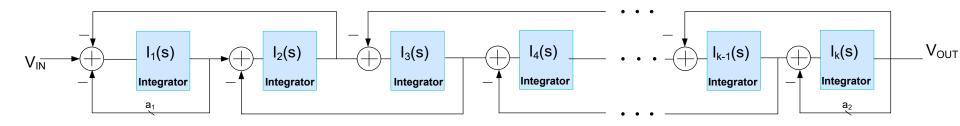
Leapfrog Filters



Introduced by Girling and Good, Wireless World, 1970

This structure has some very attractive properties and is widely used though the real benefits and limitations of the structure are often not articulated

Leapfrog Filters



Observation: This structure appears to be dramatically different than anything else ever reported and it is not intuitive why this structure would serve as a filter, much less, have some unique and very attractive properties

To understand how the structure arose, why it has attractive properties, and to identify limitations, some mathematical background is necessary

Background Information for Leapfrog Filters



Assume the impedance R_S is fixed

Theorem 1: If the LC network delivers maximum power to the load at a frequency ω , then

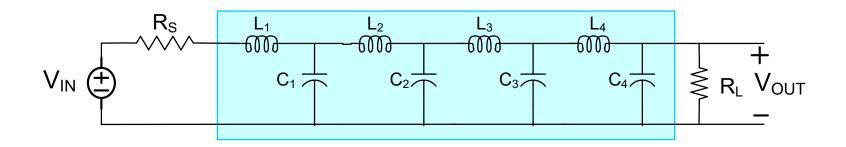
for any circuit element in the system except for $x = R_1$

This theorem will be easy to prove after we prove the following theorem:

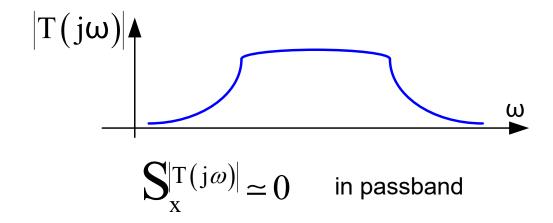
Review from last lecture

Implications of Theorem 1

Many passive LC filters such as that shown below exist that have near maximum power transfer in the passband

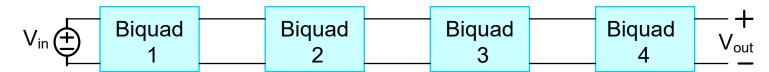


If a component in the LC network changes a little, there is little change in the passband gain characteristics (depicted as bandpass)

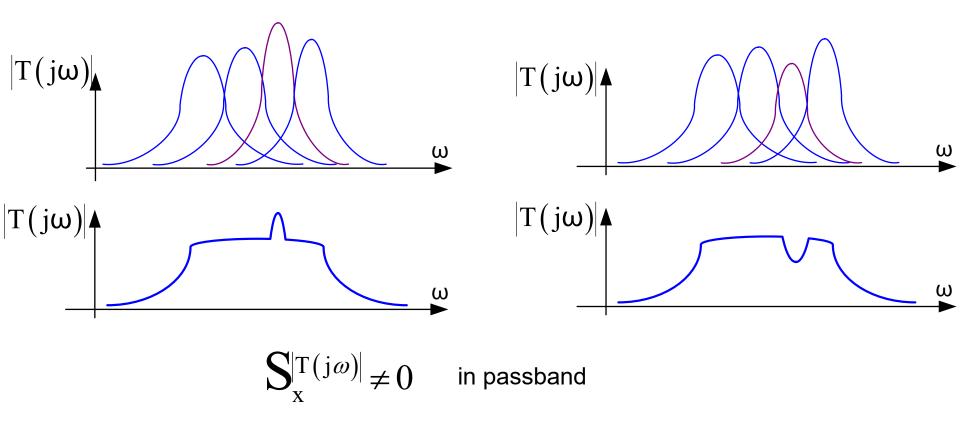


Review from last lecture

Implications of Theorem 1

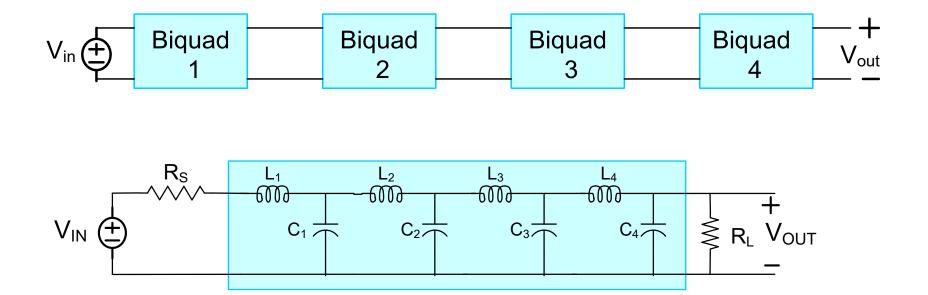


If a component in a biquad changes a little, there is often a large change in the passband gain characteristics (depicted as bandpass)



Review from last lecture

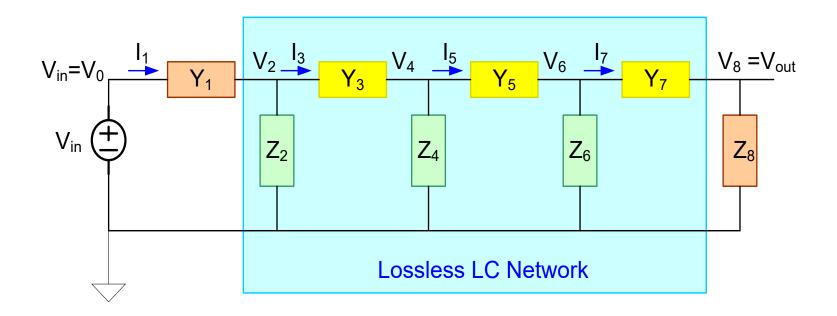
Implications of Theorem 1



Good doubly-terminated LC networks often much less sensitive to most component values in the passband than are cascaded biquads!

This is a major advantage of the LC networks but can not be applied practically in most integrated applications or even in pc-board based designs

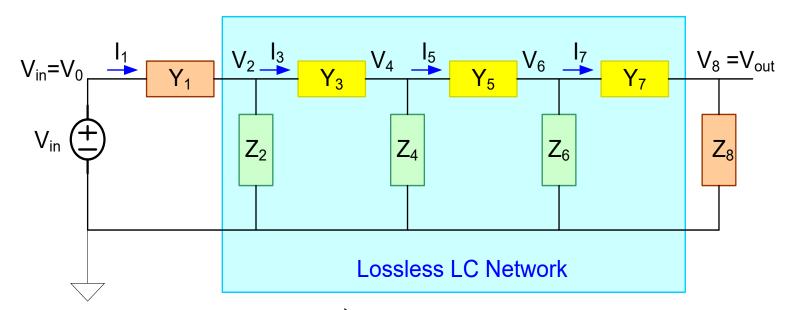
Doubly-terminated Ladder Network with Low Passband Sensitivities



For components in the LC Network observe

$$Y_k = \frac{1}{sL_k} \qquad Z_k = \frac{1}{sC_k}$$

Doubly-terminated Ladder Network with Low Passband Sensitivities



$$I_{1} = (V_{0} - V_{2}) Y_{1}$$

$$V_{2} = (I_{1} - I_{3}) Z_{2}$$

$$I_{3} = (V_{2} - V_{4}) Y_{3}$$

$$V_{4} = (I_{3} - I_{5}) Z_{4}$$

$$I_{5} = (V_{4} - V_{6}) Y_{5}$$

$$V_{6} = (I_{5} - I_{7}) Z_{6}$$

$$I_{7} = (V_{6} - V_{8}) Y_{7}$$

$$V_{8} = I_{7} Z_{8}$$

Complete set of independent equations that characterize this filter

Solution of this set of equations is tedious

All sensitivity properties of this circuit are inherently embedded in these equations!

$$I_{1} = (V_{0} - V_{2})Y_{1}$$

$$V_{2} = (I_{1} - I_{3})Z_{2}$$

$$I_{3} = (V_{2} - V_{4})Y_{3}$$

$$V_{4} = (I_{3} - I_{5})Z_{4}$$

$$I_{5} = (V_{4} - V_{6})Y_{5}$$

$$V_{6} = (I_{5} - I_{7})Z_{6}$$

$$I_{7} = (V_{6} - V_{8})Y_{7}$$

$$V_{8} = I_{7}Z_{8}$$

Rewrite the equations as

$$V'_{1} = (V_{0} - V_{2}) Y_{1}$$

$$V_{2} = (V'_{1} - V'_{3}) Z_{2}$$

$$V'_{3} = (V_{2} - V_{4}) Y_{3}$$

$$V_{4} = (V'_{3} - V'_{5}) Z_{4}$$

$$V'_{5} = (V_{4} - V_{6}) Y_{5}$$

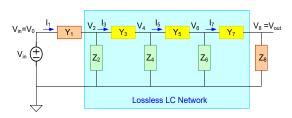
$$V_{6} = (V'_{5} - V'_{7}) Z_{6}$$

$$V'_{7} = (V_{6} - V_{8}) Y_{7}$$

$$V_{8} = V'_{7} Z_{8}$$

Make the associations

$$I_1 = V_1'$$
 $I_3 = V_3'$
 $I_5 = V_5'$
 $I_7 = V_7'$



This association is nothing more than a renaming of variables so all sensitivities WRT Y's and Z's will remain unchanged!

$$V_{1}' = (V_{0} - V_{2})Y_{1}$$

$$V_{2} = (V_{1}' - V_{3}')Z_{2}$$

$$V_{3}' = (V_{2} - V_{4})Y_{3}$$

$$V_{4} = (V_{3}' - V_{5}')Z_{4}$$

$$V_{5}' = (V_{4} - V_{6})Y_{5}$$

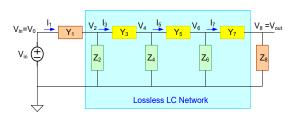
$$V_{6} = (V_{5}' - V_{7}')Z_{6}$$

$$V_{7}' = (V_{6} - V_{8})Y_{7}$$

$$V_{8} = V_{7}'Z_{8}$$

For the LC filter, recall

$$Y_k = \frac{1}{sL_k} \qquad Z_k = \frac{1}{sC_k}$$



And the source and load termination relationships were

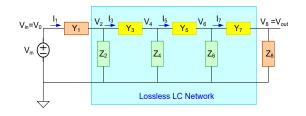
$$Y_1 = \frac{1}{R_1} \qquad Z_8 = R_8$$

These can be written as

$$\begin{aligned} V_{1}^{'} &= \left(V_{0} - V_{2}\right) \frac{1}{R_{1}} & V_{5}^{'} &= \left(V_{4} - V_{6}\right) \frac{1}{sL_{5}} \\ V_{2} &= \left(V_{1}^{'} - V_{3}^{'}\right) \frac{1}{sC_{2}} & V_{6} &= \left(V_{5}^{'} - V_{7}^{'}\right) \frac{1}{sC_{6}} \\ V_{3}^{'} &= \left(V_{2} - V_{4}\right) \frac{1}{sL_{3}} & V_{7}^{'} &= \left(V_{6} - V_{8}\right) \frac{1}{sL_{7}} \\ V_{4} &= \left(V_{3}^{'} - V_{5}^{'}\right) \frac{1}{sC_{4}} & V_{8} &= V_{7}^{'}R_{8} \end{aligned}$$

Observe that in the new parameter domain the set of intermediate equations all look like integrator functions if the primed and unprimed variables are all voltages!

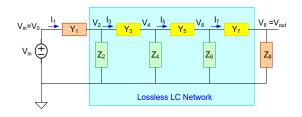
$$\begin{aligned} V_{1}^{'} &= \left(V_{0} - V_{2}\right) \frac{1}{R_{1}} & V_{5}^{'} &= \left(V_{4} - V_{6}\right) \frac{1}{sL_{5}} \\ V_{2} &= \left(V_{1}^{'} - V_{3}^{'}\right) \frac{1}{sC_{2}} & V_{6} &= \left(V_{5}^{'} - V_{7}^{'}\right) \frac{1}{sC_{6}} \\ V_{3}^{'} &= \left(V_{2} - V_{4}\right) \frac{1}{sL_{3}} & V_{7}^{'} &= \left(V_{6} - V_{8}\right) \frac{1}{sL_{7}} \\ V_{4} &= \left(V_{3}^{'} - V_{5}^{'}\right) \frac{1}{sC_{4}} & V_{8} &= V_{7}^{'}R_{8} \end{aligned}$$



Observe that in the new parameter domain the intermediate equations all look like integrator functions if the primed and unprimed variables are all voltages!

If any circuit is characterized by these equations, the sensitivities to the integrator gains will be identical to the sensitivities of the original circuit to the Ls and Cs!

$$\begin{aligned} V_{1}^{'} &= \left(V_{0} - V_{2}\right) \frac{1}{R_{1}} & V_{5}^{'} &= \left(V_{4} - V_{6}\right) \frac{1}{sL_{5}} \\ V_{2} &= \left(V_{1}^{'} - V_{3}^{'}\right) \frac{1}{sC_{2}} & V_{6} &= \left(V_{5}^{'} - V_{7}^{'}\right) \frac{1}{sC_{6}} \\ V_{3}^{'} &= \left(V_{2} - V_{4}\right) \frac{1}{sL_{3}} & V_{7}^{'} &= \left(V_{6} - V_{8}\right) \frac{1}{sL_{7}} \\ V_{4} &= \left(V_{3}^{'} - V_{5}^{'}\right) \frac{1}{sC_{4}} & V_{8} &= V_{7}^{'}R_{8} \end{aligned}$$



Each equation corresponds to either an integrator or summer with the output voltage output variables and the gain indicated (don't worry about the units)

$$\mathsf{V}_{0} - \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{R}_{1}} - \boxed{\mathsf{V}_{1}^{'}} \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{S}\mathsf{C}_{2}} - \boxed{\mathsf{V}_{2}^{'}} \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{S}\mathsf{L}_{3}} - \boxed{\mathsf{V}_{3}^{'}} \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{S}\mathsf{C}_{4}} - \boxed{\mathsf{V}_{4}^{'}} \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{S}\mathsf{L}_{5}} - \boxed{\mathsf{V}_{5}^{'}} \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{S}\mathsf{C}_{6}} - \boxed{\mathsf{V}_{6}^{'}} \boxed{\frac{+}{\mathsf{I}}}_{\mathsf{S}\mathsf{L}_{7}} - \boxed{\mathsf{V}_{7}^{'}} \boxed{\mathsf{R}}_{8} - \boxed{\mathsf{V}_{8}}$$

$$V_0 = V_{in}$$

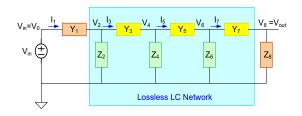
$$V_8 = V_{out}$$

$$V_{1}' = (V_{0} - V_{2}) \frac{1}{R_{1}} \qquad V_{5}' = (V_{4} - V_{6}) \frac{1}{sL_{5}}$$

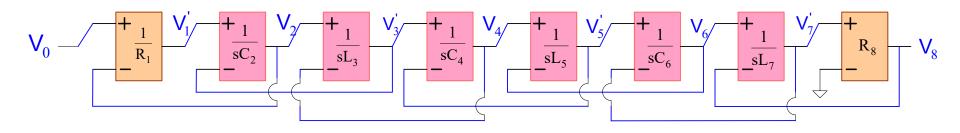
$$V_{2} = (V_{1}' - V_{3}') \frac{1}{sC_{2}} \qquad V_{6} = (V_{5}' - V_{7}') \frac{1}{sC_{6}}$$

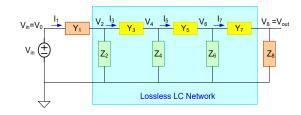
$$V_{3}' = (V_{2} - V_{4}) \frac{1}{sL_{3}} \qquad V_{7}' = (V_{6} - V_{8}) \frac{1}{sL_{7}}$$

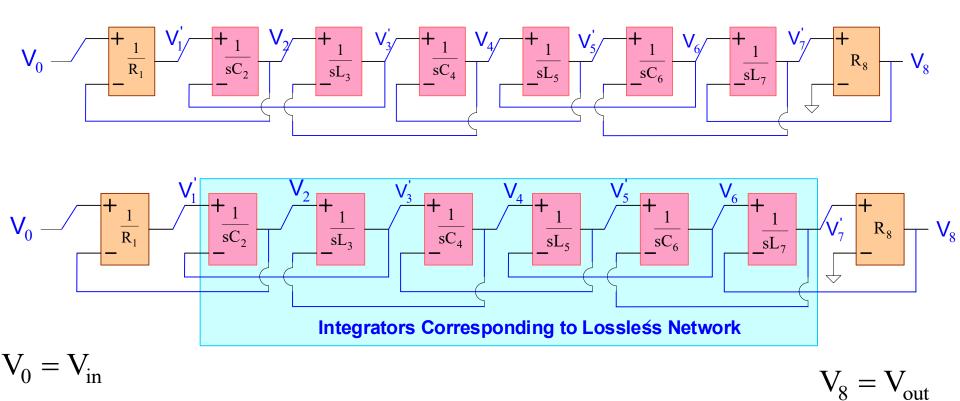
$$V_{4} = (V_{3}' - V_{5}') \frac{1}{sC_{4}} \qquad V_{8} = V_{7}'R_{8}$$



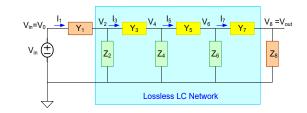
The interconnections that complete each equation can now be added

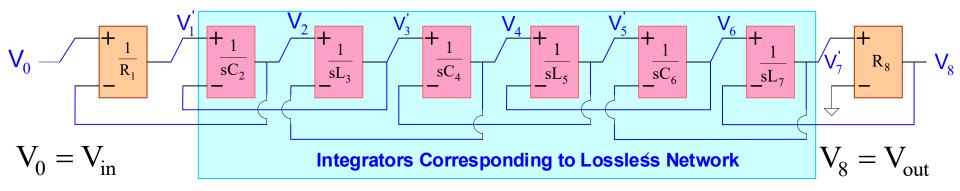




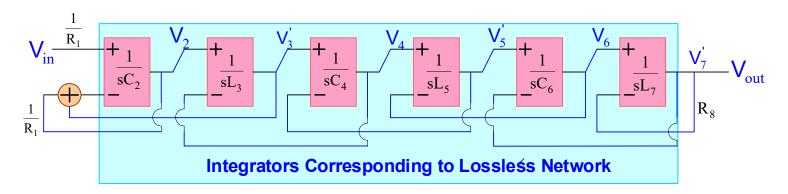


The Leapfrog Configuration

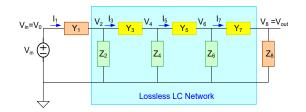


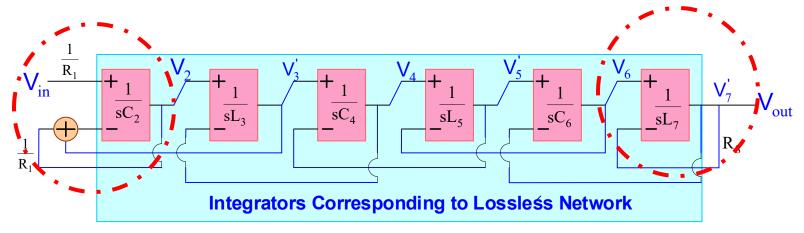


Input summing and weighting can occur at input to the first integrator The difference between V_8 and V_7 is only a scale factor that does not affect shape, and the weighting on the Vin input also does not affect shape, thus



The Leapfrog Configuration

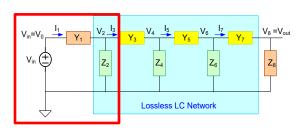


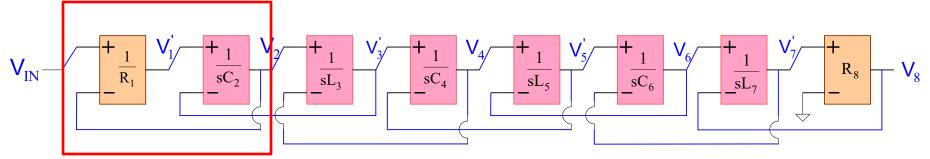


The terminations on both sides have local feedback around an integrator which can be alternately viewed as a lossy integrator

Could redraw the structure as a cascade of internal lossless integrators with terminations that are lossy integrators but since there are so many different ways to implement the integrators and summers, we will not attempt to make that association in the block diagram form but in most practical applications a lossy integrator is often used on the input or the output or both

Consider the first two stages:



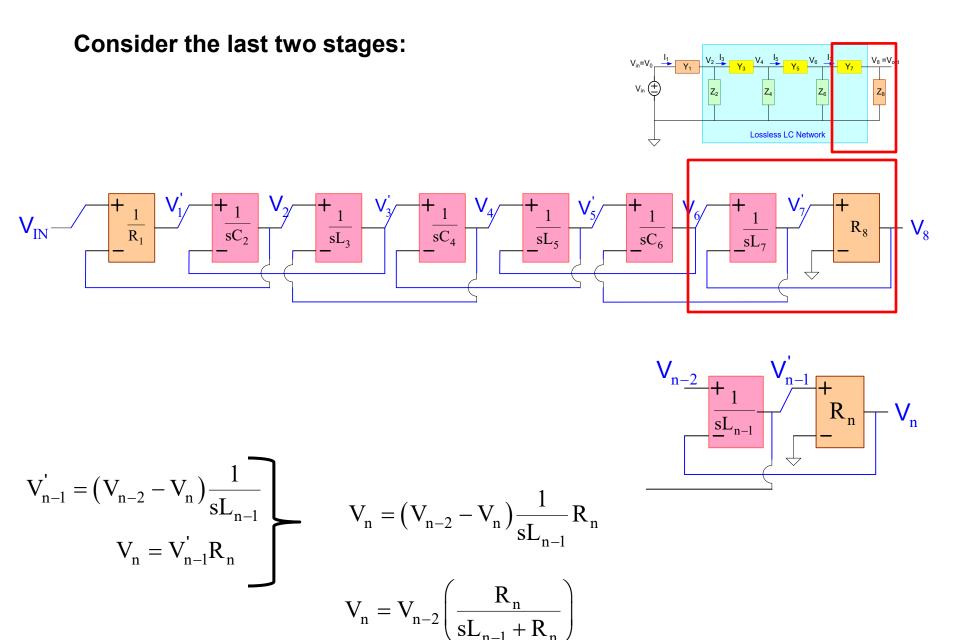


$$V_{1}' = (V_{0} - V_{2}) \frac{1}{R_{1}}$$

$$V_{2} = (V_{1}' - V_{3}') \frac{1}{sC_{2}}$$

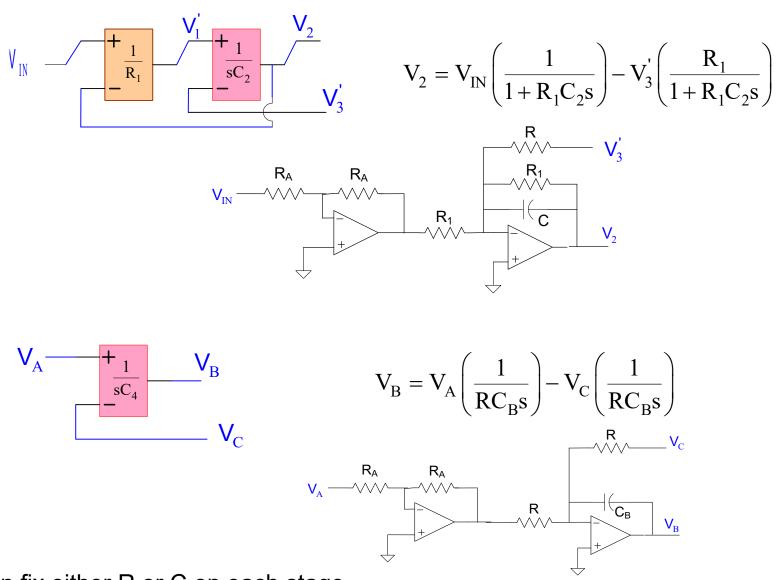
$$V_{2} = V_{IN} \left(\frac{1}{1 + R_{1}C_{2}s}\right) - V_{3}' \left(\frac{R_{1}}{1 + R_{1}C_{2}s}\right)$$

These two blocks act as a single summing lossy integrator block with loss factor R₁



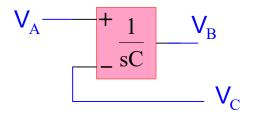
These two blocks act as a lossy integrator block with loss factor R_n

Implementation with Miller Integrators:

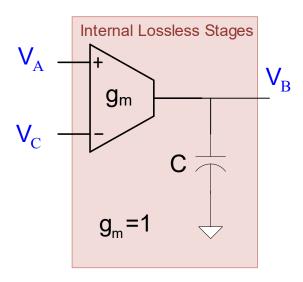


Can fix either R or C on each stage

Implementation with OTA-C Integrators:

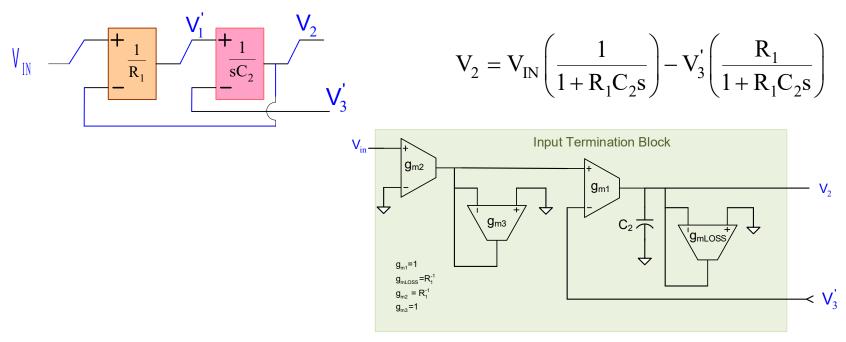


$$V_{B} = V_{A} \left(\frac{1}{sC}\right) - V_{C} \left(\frac{1}{sC}\right)$$

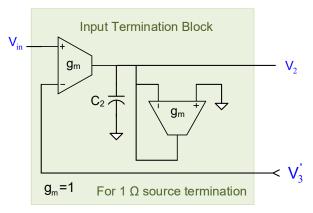


Can fix either g_m or C on each stage (showing here for $g_m=1$)

Implementation with OTA-C Integrators:

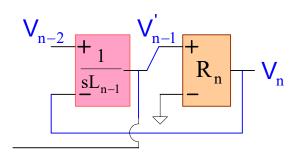


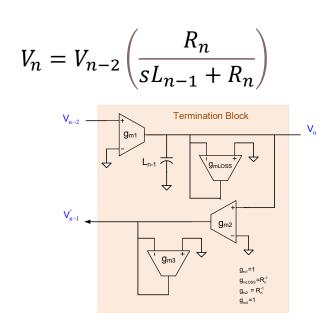
For 1 Ω source termination this simplifies to:



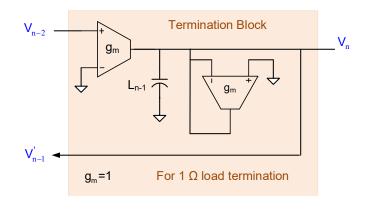
Can fix either g_m or C on each stage (showing here for $g_m=1$)

Implementation with OTA-C Integrators:



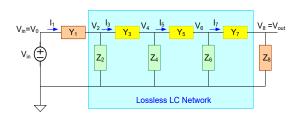


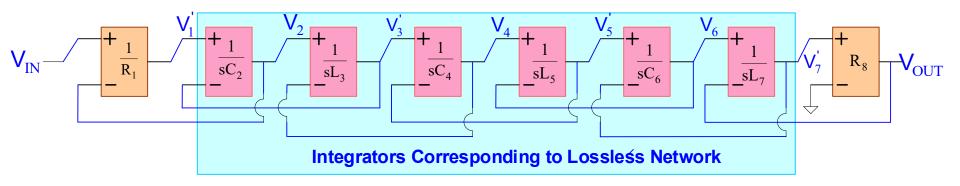
For 1 Ω load termination this simplifies to:



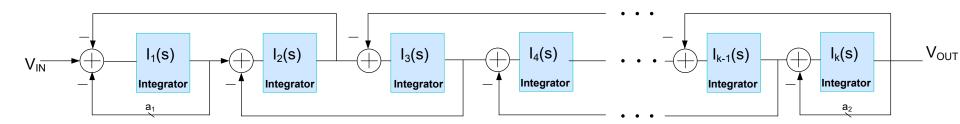
Can fix either g_m or C on each stage (showing here for $g_m=1$)

The Leapfrog Configuration



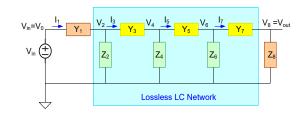


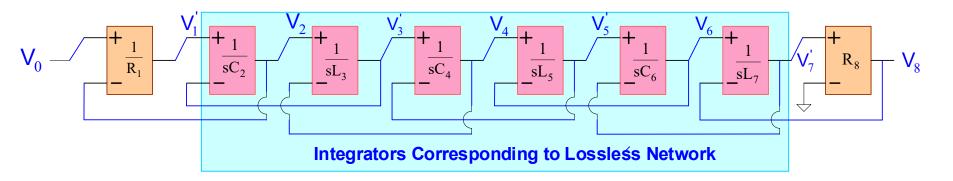
In the general case, this can be redrawn as shown below



Note the first and last integrators become lossy because of the local feedback

The Leapfrog Configuration





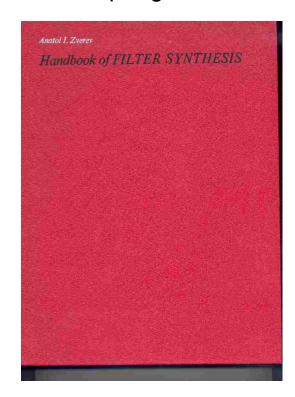
The passive prototype filter from which the leapfrog was designed has all shunt capacitors and all series inductors and is thus lowpass.

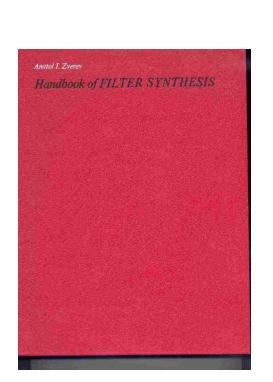
The resultant leapfrog filter has the same transfer function and is thus lowpass

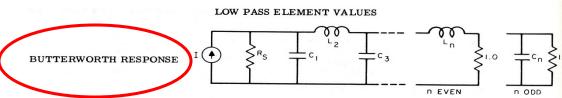
Doubly-terminated LC filters with near maximum power transfer in the passband were developed from the 30's to the 60's

Seldom discussed in current texts but older texts and occasionally software tools provide the passive structures needed to synthesize leapfrog networks

One good book is that by Zverev

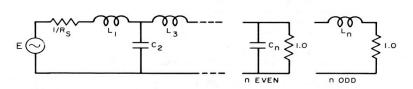




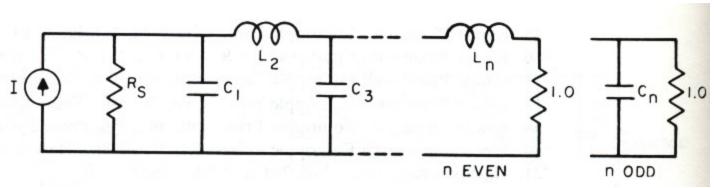


					- 37
n	Rs	C ₁	L ₂	С3	L ₄
2	1.0000 1.1111 1.2500 1.4286 1.6667 2.0000 2.5000 3.3333 5.0000 10.0000	1.4142 1.0353 0.8485 0.6971 0.5657 0.4483 0.3419 0.2447 0.1557 0.0743 1.4142	1.4142 1.8352 2.1213 2.4387 2.8284 3.3461 4.0951 5.3126 7.7067 14.8138 0.7071		
3	1.0000 0.9000 0.8000 0.7000 0.6000 0.5000 0.4000 0.3000 0.2000 0.1000 INF.	1.0000 0.8082 0.8442 0.9152 1.0225 1.1811 1.4254 1.8380 2.6687 5.1672 1.5000	2.0000 1.6332 1.3840 1.1652 0.9650 0.7789 0.6042 0.4396 0.2842 0.1377 1.3333	1.0000 1.5994 1.9259 2.2774 2.7024 3.2612 4.0642 5.3634 7.9102 15.4554 0.5000	
4	1.0000 1.1111 1.2500 1.4286 1.6667 2.0000 2.5000 3.3333 5.0000 10.0000 INF.	0.7654 0.4657 0.3657 0.3882 0.3251 0.2690 0.2175 0.1692 0.1237 0.0904 0.0392 1.5307	1.8478 1.5924 1.6946 1.8618 2.1029 2.4524 2.9858 3.8826 5.6835 11.0942 1.5772	1.8478 1.7439 1.5110 1.2913 1.0824 0.8826 0.6911 0.5072 0.3307 0.1616 1.0824	0.7654 1.4690 1.8109 2.1752 2.6131 3.1868 4.0094 5.3381 7.9397 15.6421 0.3827
n	1/R _s	L ₁	C ₂	L ₃	C ₄

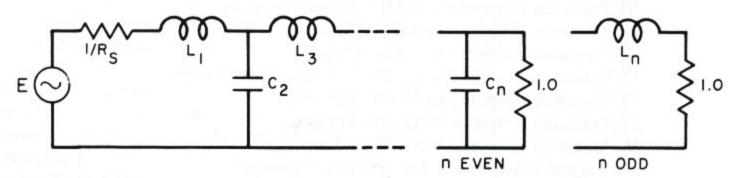
Must start with correct filter type: (e.g. BW, CC, Cauer)



The Butterworth Low-Pass Filters



First element is capacitor (appear from top to bottom in table)



First element is inductor

(appear from bottom to top in table)

Can do Thevenin-Norton Transformations

n	R _s	C ₁	L ₂	C ₃	L ₄
2	1.0000 1.111 1.2500 1.4286 1.6667 2.0000 2.5000 3.3333 5.0000 10.0000	1.4142 1.0353 0.8485 0.6971 0.5657 0.4483 0.3419 0.2447 0.1557 0.0743 1.4142	1.4142 1.8352 2.1213 2.4387 2.8284 3.3461 4.0951 5.3126 7.7067 14.8138 0.7071		
3	1.0000 0.9000 0.8000 0.7000 0.6000 0.5000 0.4000 0.3000 0.2000 0.1000 INF.	1.0000 0.8082 0.8442 0.9152 1.0225 1.1811 1.4254 1.8380 2.6687 5.1672 1.5000	2.0000 1.6332 1.3840 1.1652 0.9650 0.7789 0.6042 0.4396 0.2842 0.1377 1.3333	1.0000 1.5994 1.9259 2.2774 2.7024 3.2612 4.0642 5.3634 7.9102 15.4554 0.5000	
4	1.0000 1.1111 1.2500 1.4286 1.6667 2.0000 2.5000 3.3333 5.0000 10.0000 INF.	0.7654 0.4657 0.3882 0.3251 0.2690 0.2175 0.1692 0.1237 0.0804 0.0392 1.5307	1.8478 1.5924 1.6946 1.8618 2.1029 2.4524 2.9858 3.8826 5.6835 11.0942 1.5772	1.8478 1.7439 1.5110 1.2913 1.0824 0.8826 0.6911 0.5072 0.3307 0.1616 1.0824	0.7654 1.4690 1.8109 2.1752 2.6131 3.1868 4.0094 5.3381 7.9397 15.6421 0.3827
n	1/R _s	L ₁	С ₂	L ₃	C ₄

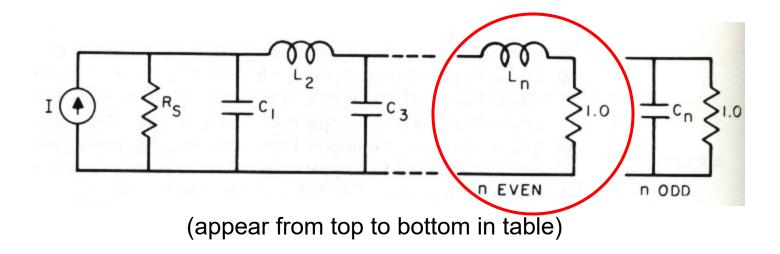
Normalized so R_L=1

n	Rs	C ₁	L ₂	С3	L ₄	C ₅	L ₆	C ₇
	1.0000	0.6180	1.6180	2,0000	1.6180	0.6180		
	0.9000	0.4416	1.0265	1.9095	1.7562	1.3887		
	0.8000	0.4698	0.8660	2.0605	1.5443	1.7380		3
	0.7000	Q.5173	0.7313	2.2849	1.3326	2.1083		
	0.6000	0.5860	0.6094	2.5998	1.1255	2.5524		
5	0.5000	0.6857	0.4955	3.0510	0.9237	3.1331	2 7 25	
	0.4000	0.8378	0.3877	3.7357	0.7274	3.9648	-	
	0.3000	1.0937	0.2848	4.8835	0.5367	5.3073		
	0.2000	1.6077	0.1861	7.1849	0.3518	7.9345		5
	0.1000	3.1522	0.0912	14.0945	0.1727	15.7103		
	INF.	1.5451	1.6944	1.3820	0.8944	0.3090		15.5
	1,0000	0.5176	1.4142	1.9319	1 0710	1.4142	0.5376	
		5			1.9319		0.5176	
	1.1111	0.2890	1.0403	1.3217	2.0539	1.7443	1.3347	
	1.4286	0.2445	1.1163	1.1257	2.2389	1.5498	1.6881	
	1.6667		1.2363	0.9567	2.4991	1.3464	2.0618	
6	2.0000	0.1732	1.4071	0.8011	2.8580	1.1431	2.5092	
U	2.5000	0.1108	2.0275	0.6542	3.3687	0.9423	3.0938	1
	3.3333	0.0816	2.6559	0.3788	4.1408 5.4325	0.7450	3.9305	1
	5.0000	0.0535	3.9170	0.2484	8.0201	0.3628	5.2804 7.9216	
	10.0000	0.0263	7.7053	0.1222	15.7855	0.1788	15.7375	
	INF.	1.5529	1.7593	1.5529	1.2016	0.7579	0.2588	
,0			10.575		1,2010	5,61313	0.2300	
	1.0000	0.4450	1.2470	1.8019	2,0000	1.8019	1.2470	0.4450
	0.9000	0.2985	0.7111	1.4043	1.4891	2.1249	1.7268	1.2961
	0.8000	0.3215	0.6057	1.5174	1.2777	2.3338	1.5461	1.6520
	0.7000	0.3571	0.5154	1.6883	1.0910	2.6177	1.3498	2.0277
	0.6000	0.4075	0.4322	1.9284	0.9170	3.0050	1.1503	2.4771
7	0.5000	0.4799	0.3536	2.2726	0.7512	3.5532	0.9513	3.0640
	0.4000	0.5899	0.2782	2.7950	0.5917	4.3799	0.7542	3.9037
	0.3000	0.7745	0.2055	3.6706	0.4373	5.7612	0.5600	5.2583
	0.2000	1.1448	0.1350	5.4267	0.2874	8.5263	0.3692	7.9079
	0.1000	2.2571	0.0665	10.7004	0.1417	16.8222	0.1823	15.7480
	INF.	1.5576	1.7988	1.6588	1.3972	1.0550	0.6560	0.2225
n	$1/R_s$	L ₁	C ₂	L ₃	C ₄	L ₅	C ₆	L ₇

Example:

Design a 6th-order BW lowpass Leapfrog filter with equal source and load terminations, and with a 3dB band edge of 4KHz.

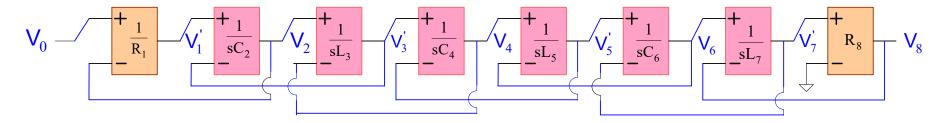
Start with the normalized BW lowpass filter



Do Norton to Thevenin transformation at input

	T	T						
n	Rs	C ₁	L ₂	C ₃	L ₄	C ₅	L ₆	C ₇
	7 0000	0 67.00	3 63.00	0,0000	7 0700	0 67.00		
	1.0000	0,6180	1,6180	2,0000	1,6180	0,6180		
	0.9000	0.4416	1.0265	1.9095	1.7562	1.3887		
	0.8000	0.4698	0.8660	2.0605	1.5443	1.7380		
	0.7000	Q.5173	0.7313	2.2849	1.3326	2.1083		
5	0.6000	0.5860	0.6094	2.5998	1.1255	2.5524		
3	0.5000	0.6857	0.4955	3.0510	0.9237	3.1331	- 1 - 1	
	0.4000	0.8378	0.3877	3.7357	0.7274	3.9648		
	0.3000	1.0937	0.2848	4.8835	0.5367	5.3073		
	0.2000	1.6077	0.1861	7.1849	0.3518	7.9345		
	0.1000	3.1522	0.0912	14.0945	0.1727	15.7103		
	INF.	1.5451	1.6944	1.3820	0.8944	0.3090		45 6 4.
	1.0000	0.5176	1.4142	1.9319	1.9319	1.4142	0.5176	
55.	1.2500	0.2445	1.1163	1.1257	2.2389	1.5498	1.6881	
	1.4286	0.2072	1.2363	0.9567	2.4991	1.3464	2.0618	
	1.6667	0.1732	1.4071	0.8011	2.8580	1.1431	2.5092	
6	2.0000	0.1412	1.6531	0.6542	3.3687	0.9423	3.0938	
	2.5000	0.1108	2.0275	0.5139	4.1408	0.7450	3.9305	
	3.3333	0.0816	2.6559	0.3788	5.4325	0.5517	5.2804	1
	5.0000	0.0535	3.9170	0.2484	8.0201	0.3628	7.9216	
	10.0000	0.0263	7.7053	0.1222	15.7855	0.1788	15.7375	1
	INF.	1.5529	1.7593	1.5529	1.2016	0.7579	0.2588	
,0								
	1.0000	0.4450	1.2470	1.8019	2,0000	1.8019	1.2470	0.4450
	0.9000	0.2985	0.7111	1.4043	1.4891	2.1249	1.7268	10 10 10 10 10 10 10 10 10 10 10 10 10 1
	0.8000	0.3215	0.6057	1.5174	1.2777	2.3338		1.2961
	0.7000	0.3571	0.5154	1.6883	1.0910	2.6177	1.5461	1.6520
	0.6000	0.4075	0.4322	1.9284	0.9170		1.3498	2.0277
7	0.5000	0.4799	0.3536	2.2726	0.7512	3.0050	1.1503	2.4771
	0.4000	0.5899	0.2782	2.7950	0.7312	3.5532 4.3799	0.9513	3.0640
	0.3000	0.7745	0.2055	3.6706	0.4373	5.7612		3.9037
	0.2000	1.1448	0.1350	5.4267	0.4373	8.5263	0.5600	5.2583
	0.1000	2.2571	0.0665	10.7004	0.1417	16.8222	0.3692	7.9079 15.7480
	INF.	1.5576	1.7988	1.6588	1.3972	1.0550	0.6560	0.2225
n	1/R _s	Ţ.	С	T.	C	Т		-
	s I	$^{ m L}_{ m 1}$	$^{\mathrm{C}}_{2}$	L ₃	C ₄	L ₅	С ₆	L ₇

 R_s =1, C_1 =.5176, L_2 =1.414, C_3 =1.939, L_4 =1.9319, C_5 =1.4142, L_6 =0.5176 Note index differs by 1 from that used for Leapfrog formulation



Labeled voltages are single-ended voltages at "+" inputs to the integrators

Changing the index notation:

$$R_1=1$$
, $C_2=.5176$, $L_3=1.414$, $C_4=1.939$, $L_5=1.9319$, $C_6=1.4142$, $L_7=0.5176$

Implement in the technology of choice

Combine loss on input and output integrators to eliminate two stages

Do frequency denormalization to obtain band-edge at 4KHz

Do impedance scaling to obtain acceptable component values

Bandpass Leapfrog Structures

Consider lowpass to bandpass transformations

Un-normalized

$$s_n \rightarrow \frac{s^2 + \omega_0^2}{sBW}$$

$$\frac{1}{s_n} \rightarrow \frac{sBW}{s^2 + \omega_0^2}$$

$$\frac{1}{s_n + \alpha} \to \frac{sBW}{s^2 + s\alpha BW + \omega_0^2}$$

Normalized

$$s_n \rightarrow \frac{s^2 + 1}{sBW_n}$$

$$\frac{1}{s_n} \to \frac{sBW_n}{s^2 + 1}$$

$$\frac{1}{s_n + \alpha} \to \frac{sBW_n}{s^2 + s\alpha BW_n + 1}$$

Bandpass Leapfrog Structures

Bandpass Leapfrog Structure obtained by replacing integrators by the corresponding transformed block

Zero sensitivity to parameters in the transformed blocks will be retained at the image frequencies of the bandpass filter

$$s_n \rightarrow \frac{s^2 + \omega_0^2}{sBW}$$

$$\frac{1}{s_n} \to \frac{sBW}{s^2 + \omega_0^2}$$

$$\frac{1}{s_n + \alpha} \rightarrow \frac{sBW}{s^2 + s\alpha BW + \omega_0^2}$$

Integrators map to bandpass biquads with infinite Q

Lossy integrators map to bandpass biquads with finite Q

Bandpass Leapfrog Structures

Bandpass Leapfrog Structure obtained by replacing integrators by the corresponding transformed block

Zero sensitivity to parameters in the transformed blocks will be retained at the image frequencies of the bandpass filter

$$\frac{1}{s_n} \to \frac{sBW}{s^2 + \omega_0^2}$$

Integrators map to bandpass biquads with infinite Q

$$\frac{1}{s_n + \alpha} \to \frac{sBW}{s^2 + s\alpha BW + \omega_0^2}$$

Lossy integrators map to bandpass biquads with finite Q

Invariably the resistance spread or the capacitance spread increases with Q

- Does this imply that the area will get very large if Q gets large?
- But what about infinite Q?
- Will infinite Q biquads be unstable?
- Is this a problem?



Stay Safe and Stay Healthy!

End of Lecture 33